

WEST BENGAL STATE UNIVERSITY

B.Sc. Honours 5th Semester Examination, 2022-23

MTMADSE01T-MATHEMATICS (DSE1/2)

LINEAR PROGRAMMING

Time Allotted: 2 Hours

Full Marks: 50

The figures in the margin indicate full marks. Candidates should answer in their own words and adhere to the word limit as practicable. All symbols are of usual significance.

Answer Question No. 1 and any five from the rest

Answer any five questions from the following:

 $2 \times 5 = 10$

- (a) Prove that the vectors (1,1,0), (0,1,1) and (1,2,1) form a basis in E^3 .
- (b) Check whether x = 5, y = 0, z = -1 is a basic solution of the system of equations:

$$x+2y+z=4,$$

$$2x+y+5z=5$$

- (c) If $C(X) = \{(x, y) : |x| \le 2, |y| \le 1\}$ be a convex hull then find set X.
- (d) Find graphically the feasible space, if any, of the following:

$$x_1 + 2x_2 \ge 2$$

 $5x_1 + 3x_2 \le 15, x_1, x_2 \ge 0$

- (e) Define fair game and strictly determinate game.
- (f) Find the maximum number of possible way of assignment of a 5×5 assignment problem.
- (g) What is the criterion for no feasible solution in two-phase method?
- (h) Define saddle point. Find the value of the game of the pay-off matrix

	Player Q				
		B_1	B_2		
Player P	A_1	1_	-1		
	A_2	-1	1		

2. A business manager has the option of investing money in two plans. Plan A guarantees that each rupee invested will earn 70 paise a year and plan B guarantees that each rupee invested will earn Rs. 2.00 every two years. In plan B, only investments for periods that are multiples of 2 years are allowed. How should the manager invest Rs. 50,000/- to maximize the earnings at the end of 3 years? Formulate the problem as a Linear Programming Problem with two legitimate variable. Find the optimum solution using graphical method.

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3. State and prove fundamental theorem of LPP.

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- 4. Use Two Phase method to solve the following linear programming problem:
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Maximize
$$z = 2x_1 + x_2 + x_3$$

Subject to
$$4x_1 + 6x_2 + 3x_3 \le 8$$

$$3x_1 - 6x_2 - 4x_3 \le 1$$

$$2x_1 + 3x_2 - 5x_3 \ge 4$$

$$x_1, x_2, x_3 \ge 0$$

- 5. (a) Prove that the set of all convex combination of a finite number of points is a convex.
- 4
- (b) Reduce the feasible solution (1, 2, 1) of the following system of equation to a basic feasible solution.

$$x_1 - x_2 + 2x_3 = 1$$

$$x_1 + 2x_2 - x_3 = 4$$

6. State and prove fundamental theorem of duality.

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Solve the following LPP using duality theory:
Minimize
$$z = x_1 + x_2 + x_3$$

7.

Subject to
$$x_1 - 3x_2 + 4x_3 = 5$$

$$x_1 - 2x_2 \leq 3$$

$$2x_2 - x_3 \ge 4$$

 $x_1, x_2 \ge 0$ and x_3 is unrestricted in sign.

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8. (a) Find the optimal assignment and the corresponding assignment cost for the assignment problem with the following cost matrix:

	D_1	D_2	D_3	D_4	D_5
O_1	2	4	3	5	4
O_2	2 7 2 8 2	4	6	8	4
<i>O</i> ₃	2	9	8	10	4
O ₄	8	6	12	7	4
05	2	8	5	8	8

(b) Find the initial B.F.S. of the following transportation problem by VAM method hence find the optimal solution:

9. Prove that the mixed strategies p^*, q^* will be optimal strategy of the game if and only if $E(p, q^*) \le E(p^*, q^*) \le E(p^*, q)$

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10.(a) Solve graphically the following game problem:

(b) Use dominance method to reduce the payoff matrix in a 2×2 game. Hence solve it.

 $\begin{array}{c|ccccc}
B_1 & B_2 & B_3 \\
A_1 & 8 & 5 & 8 \\
A_2 & 8 & 6 & 5 \\
A_3 & 7 & 4 & 5 \\
A_4 & 6 & 5 & 6
\end{array}$

11. In a rectangular game, the pay-off matrix is given by

Player Q $\begin{array}{c|cccc}
 & Q_1 & Q_2 & Q_3 \\
\hline
 & P_1 & 3 & 2 & -1 \\
\hline
 & Player <math>P & P_2 & 4 & 0 & 5 \\
\hline
 & P_3 & -1 & 3 & -2 \\
\hline
\end{array}$

State with justification, whether the players will choose pure or mixed strategies. Solve the game problem by converting it into a L.P.P.

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